

Name: \_\_\_\_\_

Math 211 Quiz 3

Section: 302           303

Feb 8, 2012

1. Find the indicated limit. If the limiting value is infinite, indicate whether it is  $+\infty$  or  $-\infty$ .

a.  $\lim_{x \rightarrow 1} \frac{x^2 + 4x - 5}{x^2 - 1}$     b.  $\lim_{x \rightarrow \infty} \frac{2x^2 - 3x}{x^2 - 1}$     c.  $\lim_{x \rightarrow -\infty} \frac{x^3 + x}{2x^2 + 1}$     d.  $\lim_{x \rightarrow 1^-} \frac{1}{x - 1}$

2. Compute the derivative of the given function and find the slope of the line that is tangent to its graph for the specified value of the independent variable.

a.  $f(x) = x^2 - 1$ ;  $x = -1$     b.  $g(t) = \sqrt{t}$ ;  $t = 4$

3. Show that the equation  $\sqrt{x} = x^2 + 2x - 1$  must have at least one solution on the interval  $0 \leq x \leq 1$ . *hint: use intermediate value property of continuous functions.*

**Bonus Problem.** A toy rocket rises vertically in such a way that  $t$  seconds after liftoff, it is  $h(t) = -16t^2 + 200t$  feet above the ground.

- a. How high is the rocket after 6 seconds?
- b. What is the average velocity of the rocket over the first 6 seconds?
- c. What is the velocity of the rocket at liftoff? What is its velocity after 6 seconds?