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 $329 \square$ 

Math 234 Quiz 1

Sep. 2014

1. (10 pts) Let

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$$\overrightarrow{\mathbf{a}} = \begin{pmatrix} 0 \\ 1 \\ 1 \end{pmatrix}, \overrightarrow{\mathbf{b}} = \begin{pmatrix} 1 \\ 0 \\ 1 \end{pmatrix}, \overrightarrow{\mathbf{c}} = \begin{pmatrix} 1 \\ 1 \\ 0 \end{pmatrix}.$$

Compute the triple product  $\overrightarrow{\mathbf{a}} \cdot (\overrightarrow{\mathbf{b}} \times \overrightarrow{\mathbf{c}})$ .

2. (10 pts) Let  $\overrightarrow{\mathbf{a}}$  and  $\overrightarrow{\mathbf{b}}$  be as above. Use dot product to find the angle between  $\overrightarrow{\mathbf{a}}$  and  $\overrightarrow{\mathbf{b}}$ . (*Hint:*  $\cos(60^\circ) = 1/2$ .)

**Bonus.** (5 pts) Let  $\overrightarrow{\mathbf{a}}$  and  $\overrightarrow{\mathbf{b}}$  be two vectors (not necessarily the same as above). Use dot product to prove the *parallelogram law*:

$$\|\overrightarrow{\mathbf{a}} + \overrightarrow{\mathbf{b}}\|^2 + \|\overrightarrow{\mathbf{a}} - \overrightarrow{\mathbf{b}}\|^2 = 2(\|\overrightarrow{\mathbf{a}}\|^2 + \|\overrightarrow{\mathbf{b}}\|^2).$$