1. Let $f(x, y)=e^{-x^{2}-y^{2}}$.
(1) (5 pts) Compute the gradient of $f$ at $(1,1)$.
(2) ( 2 pts ) In which direction does $f$ decrease fastest at $(1,1)$ ?
(3) ( 5 pts ) Find the linear approximation of $f$ at $(1,1)$.
(4) ( 3 pts ) Use (3) to estimate $f(1.1,1.1)$. (Note that $e^{-2} \approx 0.14$ ).
(5) ( 5 pts ) Find the equation of the tangent plane to the graph of $f$ at $(1,1)$.
(6) ( 3 pts ) Find the equation of the tangent line to the level curve of $f$ at $(1,1)$.
(7) (2 pts) Sketch the graph of $f$.

The last two questions are for bonus.

