Answers:

1. $f(x) = \frac{x^3}{3} + \cos x - 1$

2. $(a)\ f(x) = x^2 - x + \frac{1}{6}$ $(b)\ 0$ $(c)\ \frac{1}{2}$