

Math 231 Worksheet 9

1. Simplify the expression.

$$(a) \ln(2\sqrt{e}) - \ln 2$$

$$(b) \ln \frac{x^2}{x^2 - 1}$$

2. Differentiate the function.

$$(a) x(\ln x) - x$$

$$(b) e^{-x^2}$$

3. Evaluate the integral.

$$(a) \int_1^e \frac{\ln x}{x} dx$$

$$(b) \int \frac{e^{-\frac{1}{x}}}{x^2} dx$$

Answers.

1. (a) $\frac{1}{2}$ (b) $2 \ln x - \ln(x - 1) - \ln(x + 1)$

2. (a) $\ln x$ (b) $-2xe^{-x^2}$

3. (a) $\frac{1}{2}$ (let $u = \ln x$) (b) $e^{-\frac{1}{x}} + C$ (let $u = -\frac{1}{x}$)