1. (10 pts) Solve the initial value problem.

(a)
$$\frac{dy}{dx} = xy^2, \ y(0) = -2$$

(b)
$$\frac{dy}{dx} = e^y, \ y(0) = 0$$

2. (10 pts) Find the limit of the *sequence* if it converges. Otherwise explain why it diverges.

(a)
$$a_n = \frac{n^2 + n + 2}{n^2 + n}$$

(b)
$$a_n = \frac{n^2}{e^n}$$

(c)
$$a_n = \cos\left(\frac{1}{2^n}\right)$$

(d)
$$a_n = \frac{\sin(n^2)}{n}$$