**8.6**#1(c) When |x| < 1, we have  $|x^2| < 1$ , and therefore

$$\frac{1}{1-x^2} = \sum_{k=0}^{\infty} (x^2)^k = \sum_{k=0}^{\infty} x^{2k}.$$

So we can write, for  $x \in (-1, 1)$ ,

$$\frac{x}{1-x^2} = x \cdot \sum_{k=0}^{\infty} x^{2k} = \sum_{k=0}^{\infty} x^{2k+1}.$$

**8.6#2(b)** Substituting  $u = t^2$  in the formula

$$\sin(u) = \sum_{k=0}^{\infty} \frac{(-1)^k}{(2k+1)!} u^{2k+1},$$

we get

$$\sin(t^2) = \sum_{k=0}^{\infty} \frac{(-1)^k}{(2k+1)!} (t^2)^{2k+1} = \sum_{k=0}^{\infty} \frac{(-1)^k}{(2k+1)!} t^{4k+2},$$

which holds for all  $t \in \mathbb{R}$ . Integrating from 0 to x, we get

$$\int_0^x \sin(t^2)dt = \sum_{k=0}^\infty \frac{(-1)^k}{(2k+1)!} \int_0^x t^{4k+2}dt = \sum_{k=0}^\infty \frac{(-1)^k}{(2k+1)!} \cdot \frac{x^{4k+3}}{4k+3},$$

which holds for all  $x \in \mathbb{R}$ .

9.4#3(a)

$$\left(\begin{array}{c} x(t) \\ y(t) \end{array}\right) = \left(\begin{array}{c} -1 \\ 3 \end{array}\right) + \frac{t}{4} \left[ \left(\begin{array}{c} 2 \\ -5 \end{array}\right) - \left(\begin{array}{c} -1 \\ 3 \end{array}\right) \right] = \left(\begin{array}{c} \frac{3}{4}t - 1 \\ -2t + 3 \end{array}\right).$$

**9.4**#**3(b)** For instance:

$$\left(\begin{array}{c} x(t) \\ y(t) \end{array}\right) = \left(\begin{array}{c} -2\sin(t) \\ 2\cos(t) \end{array}\right).$$